

**Application of the Belton-Fruehan mass spectrometric method to study thermodynamic properties of oxide melts**

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ABSTRACT

Thermodynamic properties of oxide systems studied by the Belton-Fruehan mass spectrometric method are considered. The reliability of the component activities, the Gibbs energies, the partial and integral enthalpies of components obtained in the frame of this approach in oxide melts, is confirmed by the comparison with the data found by the various methods of high temperature chemistry.

1. INTRODUCTION

The Knudsen effusion mass spectrometric method is widely used nowadays for the determination of thermodynamic functions and for the investigation of the vaporization processes of the inorganic materials and melts at high temperatures. One of the reasons for that is the new method, that was suggested by Belton and Fruehan<sup>1</sup> to study thermodynamic properties of binary and multicomponent systems in the frame of high temperature mass spectrometric approach.

2. EXPERIMENTS

The main feature of the Belton-Fruehan method, which is characteristic of high temperature mass spectrometry, is the measurement of ratios of ion currents ( $I_i$  and  $I_j$ ) arising during ionization of not less than two gas-phase components ( $i, j$ ) in the system under study. The determination of the activity of  $i$ -component ( $a_i$ ) in the binary system, for example, can be carried out according to the following equation:

$$\ln a_i = - \int x_j d \ln (I_i / I_j), \quad (1)$$

where  $x_i$  is mole fraction of  $i$ -component.

Since the study of thermodynamic properties of the  $\text{CoO-FeO-SiO}_2$ ,  $\text{Na}_2\text{SiO}_3 - \text{K}_2\text{SiO}_3$ ,  $\text{Na}_2\text{Si}_2\text{O}_5 - \text{K}_2\text{Si}_2\text{O}_5$ ,  $\text{CaO-(K}_2\text{O + Na}_2\text{O)-SiO}_2$  systems by Belton et al. in 1973-1977, a lot of thermodynamic information was obtained based on this method such as activities of components and coefficients of component activities ( $\gamma_i$ ), the chemical potentials of components ( $\Delta \mu_i$ ), the Gibbs energies of the system ( $\Delta G$ ), the partial and integral enthalpies of formation ( $\Delta H_i$ ,  $\Delta H$ ) as well as the partial and integral entropies of formation ( $\Delta S_i$ ,  $\Delta S$ ).

Information on thermodynamic properties obtained using the Belton-Fruehan method in the various fields of high temperature chemistry is summarized in Table I. This method was used by many groups of investigators to study the main compositions of metallurgical slags:

$\text{Cu}_2\text{O-K}_2\text{O-SiO}_2$ ,  $\text{Cu}_2\text{O-Na}_2\text{O-SiO}_2$ ,  $\text{CaO-SiO}_2$ ,  $\text{CaO-Al}_2\text{O}_3\text{-SiO}_2$ ,  $\text{FeO-MgO-SiO}_2$ ;

glass-forming oxide systems:  $\text{Na}_2\text{O-B}_2\text{O}_3$ ,  $\text{Na}_2\text{O-GeO}_2$ ,  $\text{Na}_2\text{O-B}_2\text{O}_3\text{-GeO}_2$ ,  $\text{ZnO-PbO-B}_2\text{O}_3$ ,  $\text{GeO}_2\text{-P}_2\text{O}_5$ ,  $\text{RbBO}_2\text{-CsBO}_2$ ;

the systems containing natural minerals:  $\text{NaAlSi}_3\text{O}_8\text{-KAlSi}_3\text{O}_8$ ,  $\text{NaAlSi}_2\text{O}_6\text{-KAlSi}_2\text{O}_6$ ,  $(\text{Na,K})\text{AlSi}_4\text{O}_{10}\text{-(Na,K)Al}_2\text{Si}_5\text{O}_{12}$  and  $\text{NaAlSiO}_4\text{-KAlSiO}_4\text{-SiO}_2$ ;

highly refractory ceramics systems:  $\text{ZrO}_2\text{-Lu}_2\text{O}_3$ ,  $\text{ZrO}_2\text{-Y}_2\text{O}_3$ ,  $\text{HfO}_2\text{-Y}_2\text{O}_3$ ,  $\text{ZrO}_2\text{-Hf}_2\text{O}_3$ .

3. RESULTS

The agreement between the results of the determination of the activities of components and enthalpies of formation in oxide systems obtained by the mass spectrometric Belton-Fruehan and by the 'dimer-monomer' and comparison methods, as well as by the EMF technique, by the high temperature calorimetric method, by the measuring sulphide capacities and heterogeneous equilibria in slags, has been illustrated for the series of oxide systems, Table II. Comparison of the results obtained by these methods in the  $\text{Na}_2\text{O-GeO}_2$  and  $\text{CaO-SiO}_2$  systems, as an example, is shown in Figs. 1 and 2. The disagreement between the  $\text{GeO}_2$  and  $\text{CaO}$  activities, found by the various experimental approaches, including the Belton-Fruehan method, is within the accepted accuracy level.

As can be seen from Table I, vaporization of oxide systems, in addition to the processes of polymerization and dissociation, is also accompanied by the association of vapour molecular forms. That is the reason why, the main advantages of this method Eqn. (1), the use of ratios of ion currents values ( $I_i / I_j$ ) can disappear because of the necessity of raising  $I_i$  or  $I_j$  to a power, in accordance with the stoichiometry of the vaporization reaction. Semnikhin et al.<sup>21</sup> suggested different variants of using the Belton-Fruehan method when studying quasi-ternary oxide systems vaporizing with dissociation of components in the gaseous phase. They carried out the series of transformations of Eqn. (1) taking into account the complicated vapour composition of the system, which permitted this disadvantage to be overcome. Sidorov and Korobov<sup>47</sup> considered a general

**Table I Thermodynamic properties of oxide systems studied by the Belton-Fruehan mass spectrometric method (to be continued on the next page)**

Oxide system studied	Temperature, K	Vapour species	Thermodynamic functions obtained	Reference, year, authors
CoO-0.5SiO <sub>2</sub> -0.5FeO-SiO <sub>2</sub>	1723	Co, Fe, O <sub>2</sub>	a <sub>i</sub>	<sup>2</sup> 1973, Belton et al.
Na <sub>2</sub> SiO <sub>3</sub> -K <sub>2</sub> SiO <sub>3</sub>	1373	Na, K, O <sub>2</sub>	a <sub>i</sub> , Δ G	<sup>3</sup> 1974, Belton et al.
Na <sub>2</sub> Si <sub>2</sub> O <sub>5</sub> -K <sub>2</sub> Si <sub>2</sub> O <sub>5</sub>	1373	Na, K, O <sub>2</sub>	a <sub>i</sub> , Δ G	<sup>3</sup> 1974, Belton et al.
CaO-(K <sub>2</sub> O + Na <sub>2</sub> O)-SiO <sub>2</sub>	1373	Na, K, O <sub>2</sub>	a <sub>i</sub> , Δ G <sup>E</sup>	<sup>4</sup> 1977, Choudary et al.
Cu <sub>2</sub> O-K <sub>2</sub> O-SiO <sub>2</sub>	1373	Cu, K, O <sub>2</sub>	a <sub>i</sub>	<sup>5</sup> 1986, Kowalska et al.
Cu <sub>2</sub> O-Na <sub>2</sub> O-SiO <sub>2</sub>	1373	Cu, Na, O <sub>2</sub>	a <sub>i</sub>	<sup>6</sup> 1988, Kowalska et al.
CaO-SiO <sub>2</sub>	1933-2133	Ca, CaO, SiO, SiO <sub>2</sub> , O, CaSiO <sub>3</sub>	a <sub>i</sub> , Δ G	<sup>7</sup> 1991, Stolyarova et al.
CaO-Al <sub>2</sub> O <sub>3</sub> -SiO <sub>2</sub>	1833-2033	Ca, CaO, SiO, SiO <sub>2</sub> , O, CaSiO <sub>3</sub> , Al, AlO	a <sub>i</sub> , Δ G	<sup>8-10</sup> 1991, Stolyarova et al.
FeO-MgO-SiO <sub>2</sub>	1820-1980	Fe, Mg, SiO, O <sub>2</sub>	a <sub>i</sub>	<sup>11</sup> 1992, Plante et al.
LiReO <sub>4</sub> -CsReO <sub>4</sub>	833	LiReO <sub>4</sub> , CsReO <sub>4</sub> , Li <sub>2</sub> Re <sub>2</sub> O <sub>8</sub> , Cs <sub>2</sub> Re <sub>2</sub> O <sub>8</sub> , LiCsRe <sub>2</sub> O <sub>8</sub>	a <sub>i</sub> , γ <sub>i</sub>	<sup>12</sup> 1979, Lukas et al.
KReO <sub>4</sub> -RbReO <sub>4</sub>	855	KReO <sub>4</sub> , RbReO <sub>4</sub> , K <sub>2</sub> Re <sub>2</sub> O <sub>8</sub> , Rb <sub>2</sub> Re <sub>2</sub> O <sub>8</sub> , KRbRe <sub>2</sub> O <sub>8</sub>	a <sub>i</sub> , γ <sub>i</sub>	<sup>13</sup> 1979, Lukas et al.
Na <sub>2</sub> O-B <sub>2</sub> O <sub>3</sub>	1248-1373	NaBO <sub>2</sub> , Na <sub>2</sub> B <sub>2</sub> O <sub>4</sub> , B <sub>2</sub> O <sub>3</sub>	a <sub>i</sub> , Δ G, Δ H <sub>i</sub>	<sup>14</sup> 1979, Shultz et al.
Na <sub>2</sub> O-GeO <sub>2</sub>	1390-1590	Na, GeO, O <sub>2</sub>	a <sub>i</sub> , Δ G, Δ H <sub>i</sub>	<sup>15</sup> 1979, Shultz et al.
Na <sub>2</sub> O-B <sub>2</sub> O <sub>3</sub> -GeO <sub>2</sub>	1273-1373	Na, GeO, O <sub>2</sub> , NaBO <sub>2</sub> , Na <sub>2</sub> B <sub>2</sub> O <sub>4</sub> , B <sub>2</sub> O <sub>3</sub>	a <sub>i</sub> , Δ G	<sup>16-19</sup> 1979, 1980, Shultz et al.
PbO-B <sub>2</sub> O <sub>3</sub>	1050-1482	Pb, O <sub>2</sub> , PbO, Pb <sub>2</sub> O <sub>2</sub> , BO <sub>2</sub> , B <sub>2</sub> O <sub>3</sub> , PbBO <sub>2</sub> , Pb <sub>2</sub> BO <sub>3</sub> , Pb <sub>3</sub> BO <sub>4</sub> , PbB <sub>4</sub> O <sub>6</sub> , Pb <sub>2</sub> B <sub>2</sub> O <sub>5</sub>	a <sub>i</sub>	<sup>20</sup> 1987, Semenikhin et al.
ZnO-B <sub>2</sub> O <sub>3</sub>	1250-1484	Zn, O <sub>2</sub> , ZnO, B <sub>2</sub> O <sub>3</sub> , B <sub>2</sub> O <sub>2</sub> , BO <sub>2</sub>	a <sub>i</sub> , Δ H <sub>i</sub>	<sup>21</sup> 1987, Semenikhin et al.
ZnO-PbO-B <sub>2</sub> O <sub>3</sub>	1200-1430	Pb, O <sub>2</sub> , PbO, Pb <sub>2</sub> O <sub>2</sub> , BO <sub>2</sub> , B <sub>2</sub> O <sub>3</sub> , PbBO <sub>2</sub> , Pb <sub>2</sub> BO <sub>3</sub> , Pb <sub>3</sub> BO <sub>4</sub> , PbB <sub>4</sub> O <sub>6</sub> , Pb <sub>2</sub> B <sub>2</sub> O <sub>5</sub> , Zn, ZnO, B <sub>2</sub> O <sub>2</sub>	a <sub>i</sub> , γ <sub>i</sub>	<sup>21</sup> 1987, Semenikhin et al.
GeO <sub>2</sub> - P <sub>2</sub> O <sub>5</sub>	1423	GeO, P <sub>4</sub> O <sub>10</sub> , O <sub>2</sub> , PO <sub>2</sub> , GePO <sub>3</sub>	a <sub>i</sub> , Δ G	<sup>22</sup> 1990, Stolyarova et al.
RbBO <sub>2</sub> - CsBO <sub>2</sub>	764-978	RbBO <sub>2</sub> , CsBO <sub>2</sub> , Rb <sub>2</sub> B <sub>2</sub> O <sub>4</sub> , RbCsB <sub>2</sub> O <sub>4</sub>	a <sub>i</sub> , γ <sub>i</sub> , Δ G, Δ μ	<sup>23,24</sup> 1992, Kato et al.
NaAlSi <sub>3</sub> O <sub>8</sub> -KAlSi <sub>3</sub> O <sub>8</sub>	1150-1880	Na, K, O <sub>2</sub>	a <sub>i</sub> , Δ G, Δ H	<sup>25</sup> 1982, Rammensee et al. <sup>26</sup> 1985, Frazer et al. <sup>27</sup> 1983, Roges et al.

NaAlSi <sub>2</sub> O <sub>6</sub> -KAlSi <sub>2</sub> O <sub>6</sub>	1450	Na, K, O <sub>2</sub>	a <sub>i</sub>	<sup>28</sup> 1982, Frazer et al.
(Na,K)AlSi <sub>4</sub> O <sub>10</sub> - (Na,K)Al <sub>2</sub> Si <sub>5</sub> O <sub>12</sub>	1450-1850	Na, K, O <sub>2</sub>	a <sub>i</sub>	<sup>29</sup> 1985, Frazer et al.
NaAlSiO <sub>4</sub> -KAlSiO <sub>4</sub> -SiO <sub>2</sub>	1920	Na, K, O <sub>2</sub>	a <sub>i</sub> , Δ G, Δ H, Δ S	<sup>30</sup> 1987, Rammensee et al. <sup>31</sup> 1987, Frazer et al.
ZrO <sub>2</sub> -Y <sub>2</sub> O <sub>3</sub>	2773	ZrO <sub>2</sub> , ZrO, O, YO, Y	a <sub>i</sub>	<sup>32</sup> 1981, Belov et al.
ZrO <sub>2</sub> -Lu <sub>2</sub> O <sub>3</sub>	2700	ZrO <sub>2</sub> , ZrO, O, LuO, Lu	a <sub>i</sub>	<sup>32</sup> 1981, Belov et al.
HfO <sub>2</sub> -Y <sub>2</sub> O <sub>3</sub>	2843	HfO <sub>2</sub> , HfO, O, YO, Y	a <sub>i</sub>	<sup>33</sup> 1980, Belov et al.
ZrO <sub>2</sub> -Hf <sub>2</sub> O <sub>3</sub>	2773	ZrO <sub>2</sub> , ZrO, O, HfO, HfO <sub>2</sub>	a <sub>i</sub>	<sup>33</sup> 1980, Belov et al.

**Table II Agreement between thermodynamic properties of oxide systems obtained by the Belton-Fruehan mass spectrometric method and the data found by the other methods of high temperature chemistry**

Oxide system studied by the Belton-Fruehan method	Reference	Experimental method (approach) used for the comparison of thermodynamic functions	Thermodynamic functions	Reference
CaO-SiO <sub>2</sub>	7	EMF method By measuring of the sulphide capacities in slags	a <sub>i</sub>	34 35
CaO-Al <sub>2</sub> O <sub>3</sub> -SiO <sub>2</sub>	8-10	EMF method Studies of heterogenous equilibria in slags By measuring of the sulphide capacities in slags	a <sub>i</sub> , Δ G	34 36, 37 38
FeO-MgO-SiO <sub>2</sub>	11	Exchange equilibria in slags	a <sub>i</sub>	39,40
Na <sub>2</sub> O-B <sub>2</sub> O <sub>3</sub>	14	Mass spectrometric method: - dimer-monomer; - comparison method; EMF method High temperature calorimetry	a <sub>i</sub> , Δ G, Δ H <sub>i</sub>	14  41 42
Na <sub>2</sub> O-GeO <sub>2</sub>	15	Mass spectrometric method: - comparison method; EMF method High temperature calorimetry	a <sub>i</sub> , Δ G, Δ H <sub>i</sub>	15,  43 44
Na <sub>2</sub> O-B <sub>2</sub> O <sub>3</sub> -GeO <sub>2</sub>	16-19	Mass spectrometric method: - dimer-monomer; - comparison method;	a <sub>i</sub> , Δ G	17,18
PbO-B <sub>2</sub> O <sub>3</sub>	20	Mass spectrometric method: - dimer-monomer; EMF method	a <sub>i</sub>	20  45,46
NaAlSi <sub>3</sub> O <sub>8</sub> -KAlSi <sub>3</sub> O <sub>8</sub>	25,26	High temperature calorimetry	Δ H	27
HfO <sub>2</sub> -Y <sub>2</sub> O <sub>3</sub>	33	Mass spectrometric method using the equilibrium constant of the gaseous reaction	a <sub>i</sub>	33
ZrO <sub>2</sub> -Hf <sub>2</sub> O <sub>3</sub>	33	Mass spectrometric method using the equilibrium constant of the gaseous reaction	a <sub>i</sub>	33

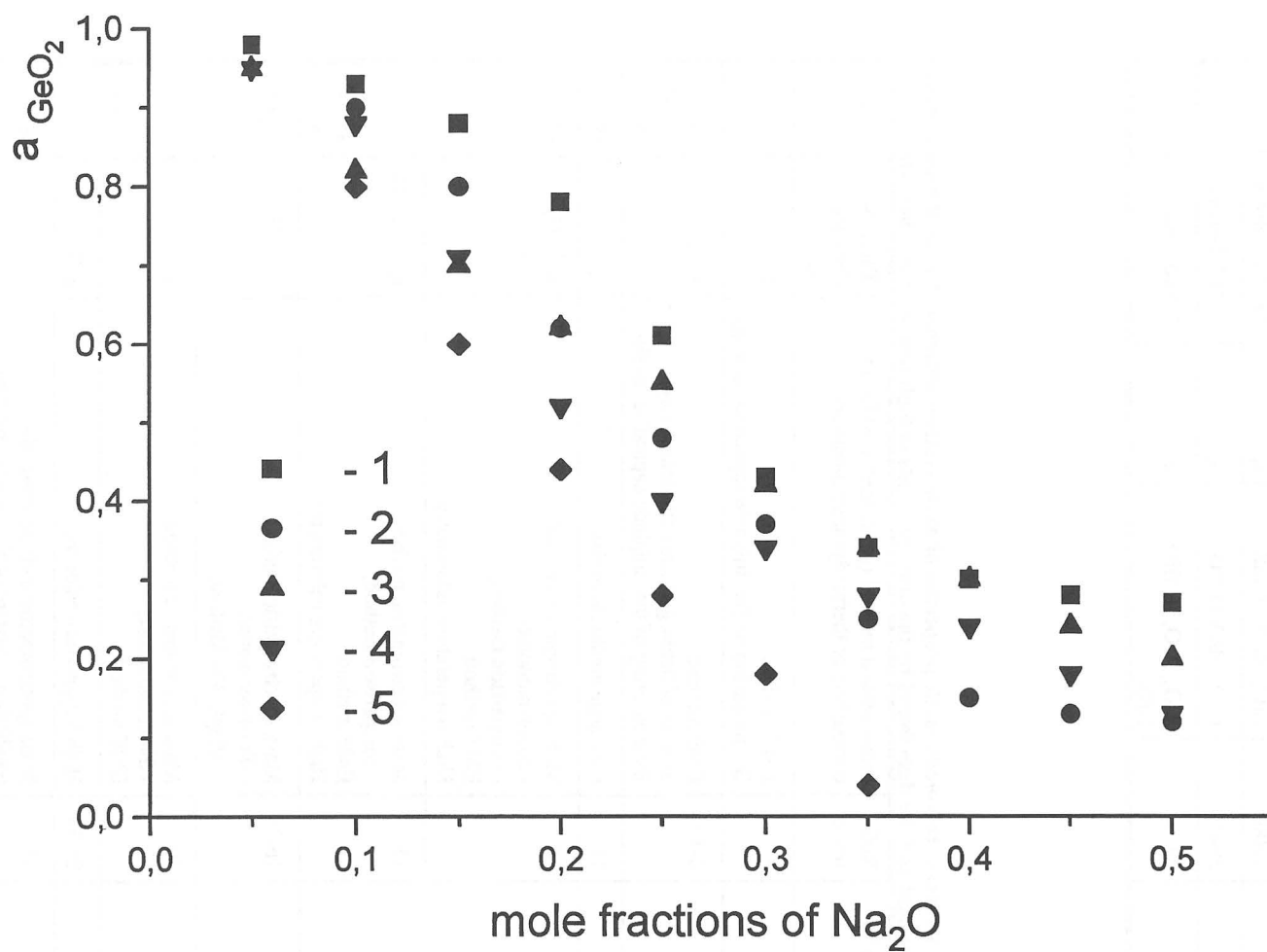


Fig. 1. The GeO<sub>2</sub> activities as a function of the concentration in the Na<sub>2</sub>O-GeO<sub>2</sub> system, obtained in the temperature range 1450-1550 K by : 1- mass spectrometric method of comparing of the ion currents<sup>15</sup>; 2- the Belton-Fruehan mass spectrometric method<sup>15</sup>; 3- the EMF method<sup>15</sup>; 4- calculated using the Gibbs-Duhem equation from the Na<sub>2</sub>O activities<sup>15</sup>; 5- the EMF method<sup>43</sup>.

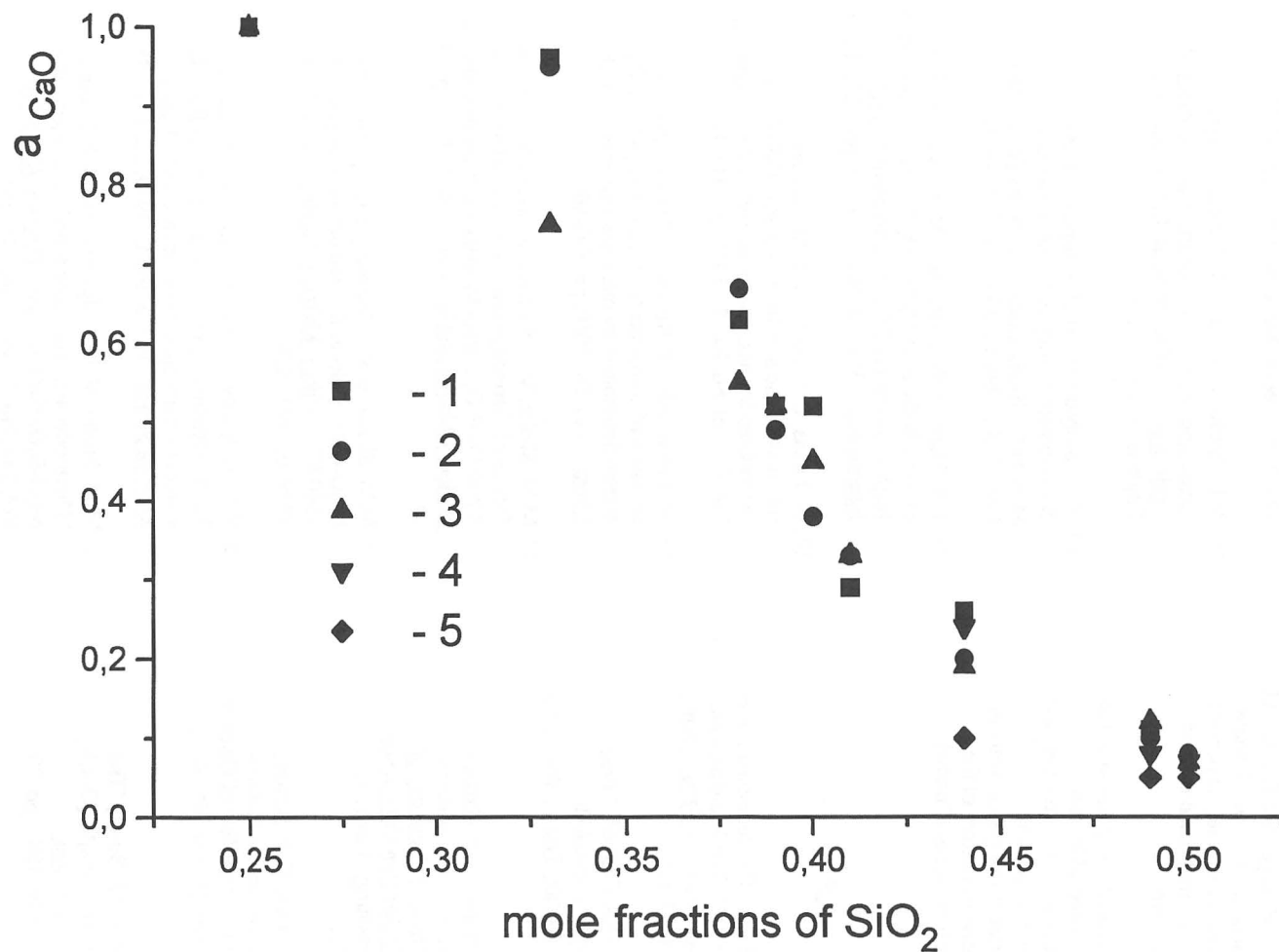


Fig. 2. The CaO activities as a function of the concentration in the CaO-SiO<sub>2</sub> system, obtained in the temperature range 1873-1933 K by : 1- mass spectrometric method of comparing of the ion currents<sup>7</sup>; 2- calculated using the Gibbs-Duhem equation from the SiO<sub>2</sub> activities<sup>7</sup>; 3- the Belton-Fruehan mass spectrometric method<sup>7</sup>; 4- the EMF method<sup>34</sup>; 5- measuring of sulphide capacities in slags<sup>35</sup>.

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